

## NUMERICAL ANALYSIS FOR COMPRESSED CERAMIC HOLLOW BRICK MASONRY COLUMNS STRENGTHENED WITH GFRP MESHES

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This article presents the analysis of obtained experimental results for the study of masonry columns which have been strengthened by GFRP confinement after high-level axial compression loading. Ceramic hollow-brick middle-scale models were investigated regarding assumed testing program. The basics of experimental studies were briefly described in the paper. Theoretical study was performed to compare experimental and theoretical values. Such numerical analysis helps to evaluate the possibility to use the existing standard's approaches for calculating bearing capacity of strengthened by GFRP jacketing ceramic brick columns which were subjected to the high axial loading. Theoretical results are rather aligned with experimental data. Some conclusions were provided in terms of usability the analytical model provided standards and other scientists. Addressing to the further investigation and research problems were performed.

**Keywords:** masonry, confinement, GFRP mesh, strengthening, effective confining pressure, design compressive strength.

### Introduction

Strengthening of compressed masonry structures by GFRP (Glass Fiber-Reinforced Polymer) meshes gains popularity due to its advantages against more typical methods (e.g. steel framing and concrete jacketing). However, polymer composites are rather new material and needs to be more investigated under different limit states and conditions.

Since the spread of composite materials from the military&space industry to the construction industry (1980s), a lot of researches have been provided to make possible to formulate the basic design provisions and approaches to design composite materials in structures. However, at present in Europe there is no single regulatory document (e.g. Eurocode) that would regulate the usage of FRP (fiber reinforced polymers) systems. The main recommendations for the use of FRP reinforcement in structures are given in the national standards of Japan (JSCE, 1997), Canada (CSA-S806, 2002), Italy (CNR-DT 200 R1/2013, 2013), USA (ACI 440.1R, 2006). The main provisions of these recommendations are highlighted in the reports of the International Reinforced Concrete Federation (FIB) regarding usage of FRP reinforcement (Matthys, & Fib Working Group, 2019). These regulations are supplemented and continued in subsequent editions.

Recently published papers (Yilmaz et al., 2013), (Cascardi et al., 2020), (Borri et al., 2012), (Valdeset al., 2015), (Witzany&Zigler, 2016) contain calculation methods analysis for the FRP confined

masonry columns. Experimental studies provided by author in scope of the tests were verified according to the existing analytical models. As result, usability of suggested approaches was discussed and accordance with experimental part was reported as well. Also, valuable inputs were provided by different scientists (Minafo et al., 2017), (Micelli et al., 2004), (Rao and Pavan, 2015), (Krevaikas and Triantafillou, 2005), (Lignova et al., 2014) in terms of analytical prediction of FRP-confined masonry structures' behavior. However, theoretical investigation for hollow ceramic brick columns strengthened with GFRP after high level loading was not provided previously.

### **Article purpose**

The purpose of this article is to evaluate existing design approaches for masonry ceramic brick columns structural analysis after high-level loading and further decompression with FRP strengthening. Also, comparative analysis between experimental and theoretical data will be performed.

### **Experimental program**

Specimens' construction, strengthening techniques and testing program were reported by authors previously in details (Bula & Kholod, 2020). The specimen's parameters were as follow: height ~ 800 mm, cross-section – 250 mm × 250 mm, mortar thickness – ~10 mm. As specimen's material the hollow ceramic bricks were used with unit dimensions 250 mm × 120 mm × 88 mm. Bonding mortar was manufactured in-site by mixing Portland cement and sand with a mass ratio of (1:6). Average (10 tests) compressive strength reported as  $f_m = 5.70$  MPa for mortar and  $f_b = 6.31$  MPa for brick. Reinforcing system included the glass fiber mesh Mapegrid G120(TM “Mapei”) and two-component ready-mixed fiber-reinforced repair mortar. Basing on producer's data mesh properties were taken as follows: mesh size – 12.7 mm × 12.7 mm; tensile strength – 1300 MPa; elastic modulus 72 GPa; ultimate strain – 1.8 %.

Masonry columns have been tested under axial compression provided by means of the hydraulic press. Specimens were axially loaded with a 10-min pause on every loading step to achieve full crack development and stabilization. Longitudinal and transversal deformations were measured by mechanical strain gages during compression test. Two columns (“s” series) were loaded up to failure as control samples. The other two columns (“d” series) were subjected to ~80 % of ultimate loading and staged for 20 min. After that the specimens were fully unloaded and confined with continuous GFRP-mesh wrapping. Preparation and strengthening application procedure was realized in accordance with producer recommendations.

### **Numerical analysis**

Numerical analysis was provided basing on Italian National Standard (CNR-DT 200 R1/2013) and on some related analytical models suggested by authors in their research (Faella et. al., 2011), (Corradi et al., 2007), (Di Ludovico et. al., 2010).

CNR standard suggests using the following equation for members confined with FRP subjected to a lateral confining pressure  $f_l$

$$f_{mcd} = f_{md} \left[ 1 + k' \left( \frac{f_{l,eff}}{f_{md}} \right)^{\alpha_1} \right], \quad (1)$$

where  $f_{mcd}$  – design compressive strength of the FRP member;  $f_{md}$  – design compressive strength of the unconfined masonry;  $k'$  – non-dimensional coefficient;  $f_{l,eff}$  – effective confining pressure;  $\alpha_1$  – coefficient equal to 0.5 if further experimental data is not available.

Non-dimensional coefficient  $k'$  is supposed to define according the equation:

$$k' = a_2 \left( \frac{g_m}{1000} \right)^{a_3}, \quad (2)$$

where  $g_m$  – masonry mass-density expressed as  $\text{kg/m}^3$ ;  $a_1$  and  $a_2$  – coefficient equal to 1.0 if further experimental data is not available.

The effective confining pressure is defined as a function of the coefficient of efficiency:

$$f_{l,eff} = k_{eff} f_l = k_H k_V f_l, \quad (3)$$

where  $k_H$  – horizontal coefficient of efficiency (depends on cross-section geometry);  $k_V$  – vertical coefficient of efficiency (depends on wrapping type);  $f_l$  – confining pressure caused by FRP material;

For a continuous confinement,  $k_V$  is equal to 1. The following equations should be used for  $f_l, k_H, k_V$  values in case of rectangular (square) cross-section and continuous FRP reinforcement:

$$f_l = 2 \frac{t_f E_f}{\max\{b, h\}} e_{f d, rid}, \quad (4)$$

where  $t_f$  – FRP thickness;  $E_f$  – FRP modulus of elasticity;  $b, h$  – columns cross-section dimensions;  $e_{f d, rid}$  – reduced design strain for FRP reinforcement.

The horizontal coefficient of efficiency is given by the ratio between the confined area and the total area of the masonry column,  $A_m$ , as follows:

$$k_H = 1 - \frac{b'^2 + h'^2}{3A_m}. \quad (5)$$

Dimensions mentioned in equation (5) are indicated in Fig. 1.

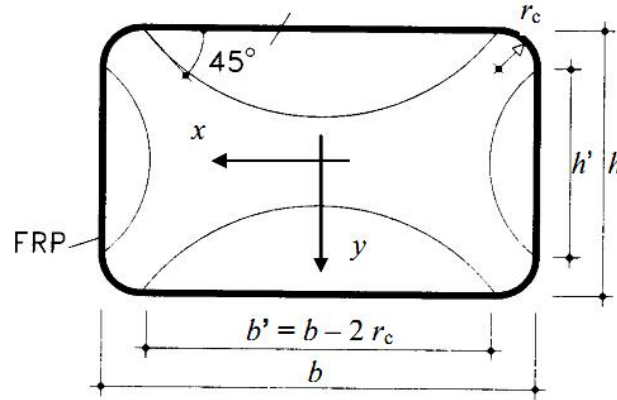


Fig. 1. Confinement of rectangular sections externally wrapped with FRP

The reduced design strain for FRP reinforcement can be written as follows:

$$e_{f d, rid} = \min \left\{ \frac{\eta_a e_{fk}}{g_f}; 0.004 \right\}, \quad (6)$$

where  $\eta_a$  – the environmental conversion factor for different exposure conditions;  $e_{fk}$  – ultimate strain for FRP mesh (technical data depends on mesh type);

$g_f$  – partial factors for FRP mesh. For the ultimate limit state, the value assigned to the partial factor of FRP materials is equal to 1.10; 0.004 – conventional strain limit.

Numerical investigations have been performed according to the equations listed above. The initial data sheet for masonry and GFRP reinforcement is given in Table 1. Compressive strength for unconfined masonry was defined by experimental data. Reinforcement characteristics were taken from producer's data sheet. Design factors were assumed according to CNR tables.

Table 1

**Masonry/Reinforcement Data Sheet**

Data	Symbol	Value	Units
Design compressive strength of the unconfined masonry (Bula & Kholod, 2020)	$f_{md}$	3.02	[MPa]
Masonry mass-density	$g_m$	1710	[kg/m <sup>3</sup> ]
Equivalent thickness of dry mesh (GFRP)	$t_f$	0.024	[mm]
Modulus of elasticity (GFRP)	$E_f$	72000	[MPa]
Elongation at failure	$e_{fk}$	1.8	[%]
Masonry column dimensions	$b \times h$	250×250	[mm]
Column's fillet	$r_c$	30	[mm]
Partial factor for GFRP mesh	$\gamma_f$	1.1	–
Environmental conversion factor	$\eta_a$	0.75	–

The design compressive strength for confined samples and comparison with experimental data are provided in Table 2. The mean value for experimental samples in series is shown. The theoretical values have been calculated for different analytical models and reported below.

Table 2

**Comparison between experimental and theoretical results**

Strengthened samples "s" series	$f_{mcd} (EXP, peak)$ mesh failure criteria [MPa]	$f_{mcd} (THEOR)$ (CNR DT 200R1/2013) [MPa]	$f_{mcd} (THEOR)$ (Faella et al.) [MPa]	$f_{mcd} (THEOR)$ (Corradi et al.) [MPa]	$f_{mcd} (THEOR)$ (Di Ludovico et al.) [MPa]
Compressive strength	4.2	3.57	4.9	3.2	3.1
<u>EXP</u> THEOR ratio	–	1.17	0.85	1.31	1.35

**Conclusions**

In this article theoretical evaluation was performed for the confined middle-scale masonry structures produced with hollow ceramic bricks after subjecting them to a high level (up to 80 % of ultimate strength) compression. Numerical investigation shows quite good compliance with experimental results (see Table 2). However, calculations by (Di Ludovico et. al., 2010) and (Corradi et al., 2007) give more conservative outcome (31–35 %) comparing with the experimental data. Analytical model by (Faella et. al., 2011) reveals 15 % overestimating of the theoretical compressive strength value. The closest agreement was received according to (CNR-DT 200 R1/2013, 2013). Such versatile theoretical results could be explained by specific hollow ceramic brick behavior, which is not fully accounted in investigated analytical models.

In general, approach proposed in CNR can be used for predicting of the compressive strength for corresponding “damages/material” combination. Although, more detailed FEM model analysis and probably existing analytical models calibration needs to be provided in further research for correspondent combination.

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### **ЧИСЕЛЬНИЙ АНАЛІЗ СТИСНУТИХ ЦЕГЛЯНИХ КОНСТРУКЦІЙ З ПУСТОТІЛОЇ КЕРАМІЧНОЇ ЦЕГЛИ, ЩО БУЛИ ПОСИЛЕНІ СІТКАМИ ІЗ СКЛОВОЛОКНА**

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Наведено чисельний аналіз експериментальних результатів, що отримані в результаті випробувань стиснутих цегляних конструкцій виконаних із пустотілої керамічної цегли, що піддавалися центральному стиску до рівня 80 % від руйнівного, розвантажувалися та підсилювалися за допомогою сіток із скловолокна.

На цей момент у Європі (як і в Україні) немає єдиного нормативного документа, що регламентує використання композитних матеріалів під час підсилення конструкцій. Основні рекомендації щодо застосування FRP армування у залізобетонних конструкціях наведено у національних нормах Японії, Канади, США. Основні положення цих рекомендацій також висвітлено у звітах Міжнародної федерації зі залізобетону (FIB) щодо використання FRP-армування.

На цей момент багато науковців проводять дослідження підсилення композитними матеріалами цегляних колон за різних рівнів навантаження, типу цегляної кладки, типу матеріалу підсилення. Отримані експериментальні результати верифікуються з теоретичними положеннями, що викладені у національних нормах окремих країн.

Проведено аналіз експериментальних результатів на основі італійських національних норм та на основі методик розрахунку, що їх запропонували деякі італійські науковці. У результаті проаналізовано збіжність експериментальних результатів з теоретичними засадами розрахунку (за чотирма методиками). Отримані збіжності експериментальних та теоретичних даних показали, що досліджувані поєднання рівня навантажень та типу кладки не повністю враховані у розрахункових підходах та потребують уточнення. Завданням таких досліджень є створення уточнених розрахункових моделей та пропозицій до розрахунку таких конструкцій.

**Ключові слова:** чисельний аналіз, цегляні конструкції, сітки із скловолокна, композитні матеріали, підсилення, міцність кладки на стиск.