

## ОЦІНКА ТОЧНОСТІ КЛАСИФІКАЦІЇ ЗА ДОПОМОГОЮ НЕЙРОМЕРЕЖІ ПРЯМОГО ПОШИРЕННЯ ДИНАМІЧНИХ ОБ'ЄКТІВ

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У даній роботі на основі мультишарової нейронної мережі досліджено вплив кількості прихованих шарів, числа нейронів у них та типів активаційних функцій на точність класифікації снарядів шістьох типів (А – (а-боєприпаси); А/М – (а/м-боєприпаси; А/Р – (бронебійні); А/РС – (бронебійно-набивні); М – (м-боєприпаси); Р – (бронебійні боєприпаси)), яка оцінюється матрицею помилок. Зокрема, побудовані матриці помилок для оцінки точності класифікації снарядів шістьох типів (А – (а-боєприпаси); А/М – (а/м-боєприпаси; А/Р – (бронебійні); А/РС – (бронебійно-набивні); М – (м-боєприпаси); Р – (бронебійні боєприпаси) мультишаровим нейронним перцептроном з одним, двома та трьома прихованими шарами та функціями активацій: Logistic, Tanh, Relu, Softmax відповідно. Встановлено, що найвища точність класифікації снарядів досягається за допомогою нейромережі з двома прихованими шарами з кількістю нейронів у першому прихованому шарі 33 з функцією активації tanh та 8-ми нейронами з функцією активації Tanh у другому прихованому шарі та Softmax для нейронів вихідного шару.

**Ключові слова:** матриця помилок, класифікація снарядів, нейронна мережа, оптимізація обчислювальних ресурсів.

### Introduction

In the modern dimension of security and defense, the important task is the classification of projectiles by their type in order to ensure the safety of citizens and effective management of military operations. Various machine learning methods, including the analysis of the confusion matrix, are used to achieve this goal. The confusion matrix is a powerful tool for evaluating the effectiveness of classifiers in tasks such as projectile type classification. This article aims to conduct a comparative analysis between different configurations of feedforward neural networks in the context of projectile classification.

The task of neural network classification of projectiles (A – (artillery), A/M – (anti-tank), A/R – (armor-piercing), A/RC – (armor-piercing-incendiary), M – (mines), R – (rockets)) is relevant, as its solution automatically solves the problem of determining the type of projectile [1] (artillery or rocket) for the selection of effective strategies and tactics in military operations, for the safe removal and disposal of unexploded projectiles, and for researching the properties and characteristics of new types of projectiles.

The article considers the application of the confusion matrix for the classification of projectiles (A – (artillery), A/M – (anti-tank), A/R – (armor-piercing), A/RC – (armor-piercing-incendiary), M – (mines), R – (rockets)) using MLP perceptron to determine the type of projectile (artillery or rocket) using neural networks with one-, two-, three-hidden layers, having respectively the number of neurons 33; 33 and 8; 33, 16 and 8 with activation functions relu, tanh, logistic.

The work examines neural networks with the following morphologies: MLPClassifier\_1HL\_L (neural network with an input sensory layer of 18 neurons, a hidden layer of 33 neurons with activation functions Logistic, an output layer of 6 neurons with activation functions Softmax), MLPClassifier\_2HL\_T (neural network with an input sensory layer of 18 neurons, the first hidden layer of 33 neurons with activation functions Tanh, the second hidden layer of 8 neurons with activation functions Tanh, an output layer of 6 neurons with activation functions Softmax), MLPClassifier\_3HL\_T (neural network with an input sensory layer of 18 neurons, the first hidden layer of 33 neurons with activation functions Tanh, the second hidden layer of 8 neurons with activation functions Tanh, the third hidden layer of 16 neurons with activation functions Tanh, an output layer of 6 neurons with activation functions Softmax), and MLPClassifier\_2HL\_R (neural network with an input sensory layer of 18 neurons, the first hidden layer of 33 neurons with activation functions Relu, the second hidden layer of 8 neurons with activation functions Relu, an output layer of 6 neurons with activation functions Softmax).

MLPClassifier\_1HL\_L is a neural network with an input sensory layer of 18 neurons, which corresponds to the 18 components of the input feature vector; a hidden layer with 33 neurons with activation functions Logistics; an output layer of 6 neurons with activation functions Softmax, as 6 objects are classified.

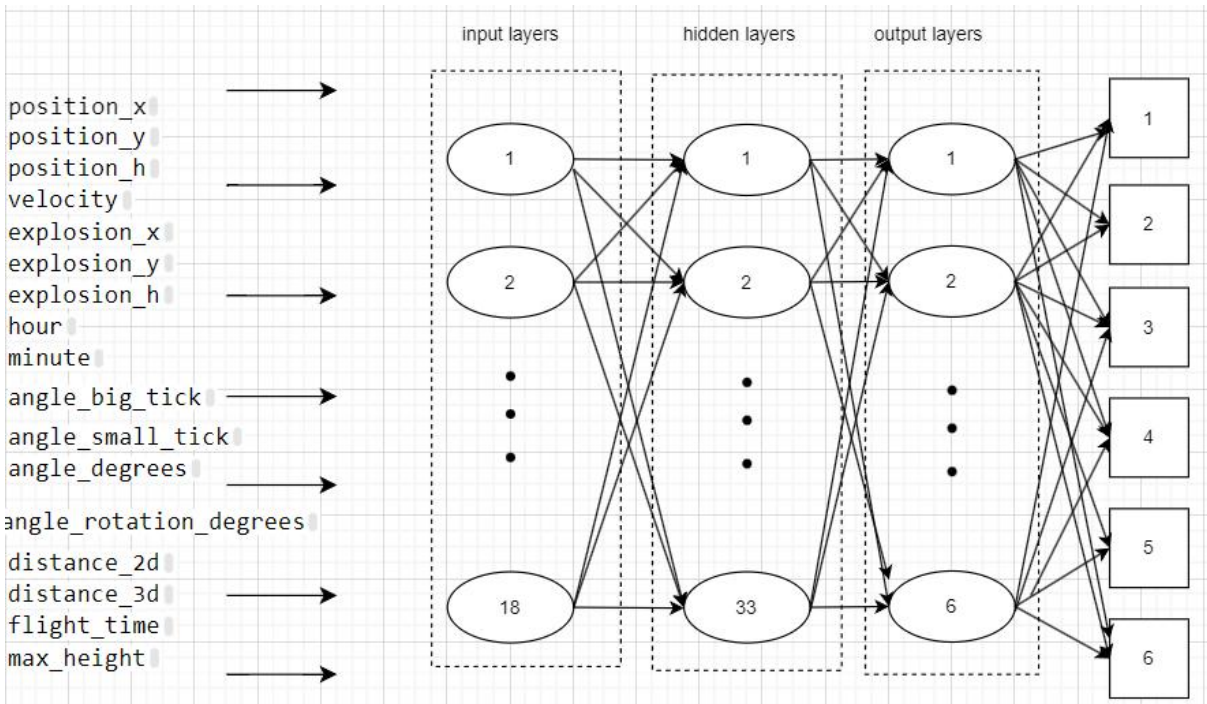


Fig. 1. Model MLPClassifier\_1HL\_L (formula (1))

$$y_i = f_{softmax} \left( \left( \sum_{j=1}^{33} w_{ij} f_{logistic} \left( \sum_{k=1}^{18} w_{jk} x_k \right) \right) \right) \quad i \in \{1; 6\}, \quad (1)$$

The architecture of the MLPClassifier\_2HL\_T neural network with two hidden layers and the Tanh activation function will be discussed in detail in the following sections, as this model was chosen for projectile classification due to its highest classification accuracy. The next model, MLPClassifier\_3HL\_T, is a neural network with an input sensory layer of 18 neurons, corresponding to the 18 components of the input feature vector; a first hidden layer of 33 neurons with activation functions Tanh; a second hidden layer of 16 neurons with activation functions Tanh; a third hidden layer of 8 neurons with activation functions Tanh; and an output layer of 6 neurons with activation functions Softmax, as 6 objects are classified.

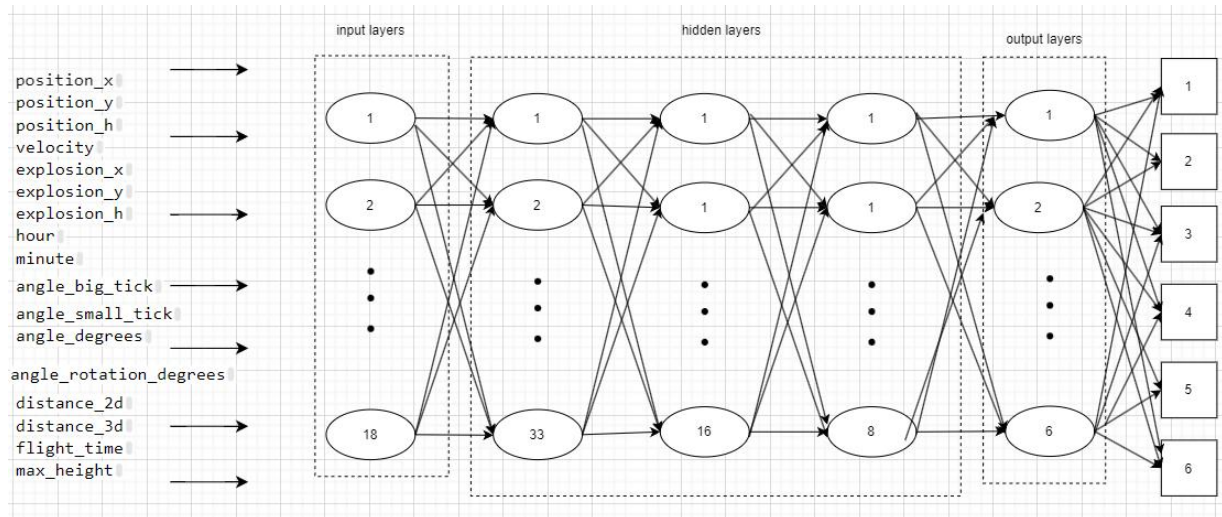


Fig. 2. Model MLPClassifier\_3HL\_T (formula (2))

$$y_i = f_{softmax} \left( \sum_{l=1}^{16} w_{ml} f_{tanh} \left( \sum_{i=1}^8 w_{li} f_{tanh} \left( \sum_{j=1}^{33} w_{ij} f_{tanh} \left( \sum_{k=1}^{18} w_{jk} x_k \right) \right) \right) \right) i \in \{1; 6\}, \quad (2)$$

It has been shown that the neural network with two hidden layers and 33 and 8 neurons with Tanh activation functions respectively, and an output layer with six neurons with a Softmax activation function, achieves the highest classification accuracy for projectiles (95.9%).

### Analysis of recent research and publications

Recent publications in the field of machine learning and neural networks have demonstrated significant advancements in various application domains. Two notable areas of focus include the optimization of neural network models and the utilization of deep learning techniques for classification tasks.

In recent studies, the optimization of neural network models has been a key area of exploration. One approach introduced is the TWD-SFNN model, which integrates the three-way decisions method with feedforward neural networks. This model dynamically determines the number of hidden layer nodes and addresses challenges such as dataset discretization and learning process adjustment.

Additionally, the application of deep neural networks (DNNs) for classification tasks has garnered attention. A recent publication explores the use of DNNs for classifying space objects using light curve data. This study compares DNN-based algorithms with traditional methods and provides insights into their effectiveness and limitations.

Recent research and publications in the field of classifier performance evaluation using the confusion matrix and other metrics include various approaches and methods to improve this process. Below are several current research directions with references to relevant articles:

1. Methods for evaluating multi-label classifiers. In the article [1], the authors discuss methods for evaluating the effectiveness of classifiers for tasks where each element can belong to multiple classes simultaneously.

2. Extension of the confusion matrix. In the work [2], the authors investigate the extension of the confusion matrix to account for additional aspects of classification and uncertainty.

3. Use of a three-way confusion matrix. In the article [2], the authors use a three-way confusion matrix to assess uncertainty in decision-making.

4. Generalization of performance metrics. In the work [3], the authors generalize performance metrics for classifiers to account for the characteristics of the classification task.

5. Application of machine learning. In the article [3], researchers use machine learning methods to improve the evaluation of classifier performance.

Overall, these studies demonstrate the continuous development and improvement of methods for evaluating classifier performance for more accurate and reliable analysis of classification results in various application areas.

### Formulation of the purpose of the article

The aim of the work is to evaluate the accuracy of projectile classification (A – (artillery), A/M – (anti-tank), A/R – (armor-piercing), A/RC – (armor-piercing-incendiary), M – (mines), R – (rockets)) using a neural network perceptron with different numbers of hidden layers, neurons in them, and different activation functions based on the confusion matrix.

### Presentation of the main material

Let  $X$  – the set of descriptions of dynamic objects (projectiles) consists of 6 types, i.e.,  $|Y| = 6$ . Each object  $x \in X$  is described by a feature vector of 18 components. The target dependency  $y^*: X \rightarrow Y$  is known only in a finite training sample  $X^m = \{(x_1, y_1), \dots, (x_m, y_m)\}$ , where  $x_i \in R^{18}$  – is a feature vector,  $y_i \in \{1, 2, 3, 4, 5, 6\}$  – is the class number (type of projectile). The task is to construct an algorithm  $a: X \rightarrow Y$ , capable of classifying any object  $x \in X$  from the 6 projectile classes with high accuracy using an optimized multilayer perceptron (with the number of hidden layers, the number of neurons in them, and the type of activation functions) based on a high-quality training sample.

For the classification of dynamic objects (A – 1, A/M – 2, A/R – 3, A/RC – 4, M – 5, R – 6), the study uses a three-layer neural network optimized by the number of hidden layers and the number of neurons in them, with the following morphology: two hidden layers and one output layer. The input sensory layer has 18 neurons, because the input feature vector has 18 components; the first hidden layer has 33 neurons with Tanh activation functions; the second hidden layer has 8 neurons with Tanh activation functions; the output layer has 6 neurons with Softmax activation functions, because there are 6 objects being classified.

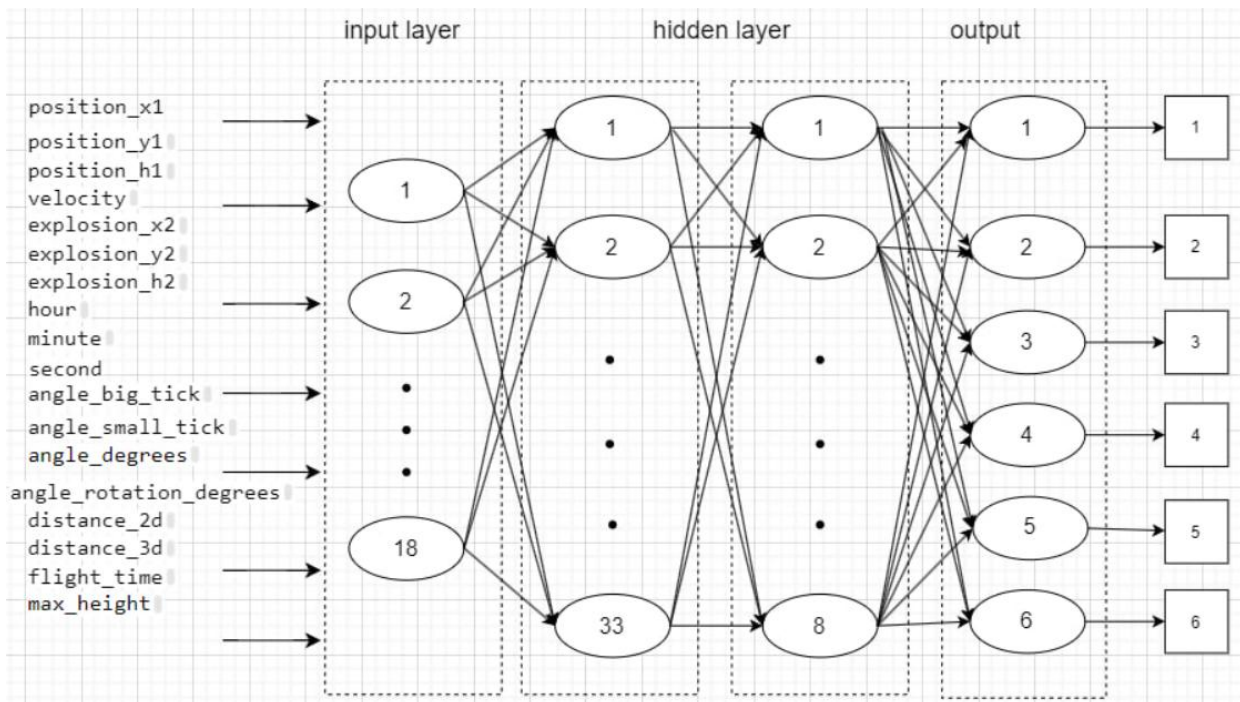


Fig. 3: Three-layer neural network model (formula(3))

Formula of the model:

$$y_i = f_{softmax} \left( \sum_{i=1}^8 w_{li} f_{tanh} \left( \sum_{j=1}^{33} w_{ij} f_{tanh} \left( \sum_{k=1}^{18} w_{jk} x_k \right) \right) \right) i \in \{1; 6\}, \quad (3)$$

where  $y_i$  – is an element of the output vector of probabilities for each class of projectiles;  $f_{softmax}$  – is the Softmax activation function;  $f_{tanh}$  – is the Tanh activation function;  $w_{li}$  – is an element of the weight matrix between the second hidden layer and the output layer;  $w_{ij}$  – is an element of the weight matrix between the first and second hidden layers;  $w_{jk}$  – is an element of the weight matrix between the input layer and the first hidden layer, the model receives the input feature vector  $\vec{x} = (x_1, x_2, \dots, x_{18})$ , where  $x_1$  – position\_x1,  $x_2$  – position\_y1,  $x_3$  – position\_h1,  $x_4$  – velocity,  $x_5$  – taget\_class,  $x_6$  – explosion\_x2,  $x_7$  – explosion\_y2,  $x_8$  – explosion\_h2,  $x_9$  – hour,  $x_{10}$  – minute,  $x_{11}$  – second,  $x_{12}$  – angle\_big\_tick,  $x_{13}$  – angle\_small\_tick,  $x_{14}$  – angle\_degrees,  $x_{15}$  – angle\_rotation\_degrees,  $x_{16}$  – distance\_2d,  $x_{17}$  – distance\_3d,  $x_{18}$  – flight\_time.

To prepare data for the classification of projectiles from the 1L220U-KS complex, the method of pseudorandom noise with a normal distribution is used to generate new values that help the MLPClassifier\_2HL\_T neural network acquire generalizing properties.

Generation of a new value (formula3)):

$$V_i^* = V_i + \sigma_i \cdot N(\mathbf{0}, \mathbf{1}), \quad (4)$$

where  $V_i^*$  – is the new value of the  $i$ -th characteristic;  $V_i$  – is the initial value of the  $i$ -th characteristic;  $\sigma_i$  – is the standard deviation of the  $i$ -th characteristic;  $N(\mathbf{0}, \mathbf{1})$  – is the function for generating pseudorandom values with a normal distribution (mean = 0, standard deviation = 1).

Calculation of the standard deviation (formula (4)):

$$\sigma_i = \sqrt{\frac{\sum (V_i - \mu_i)^2}{N}}, \quad (5)$$

where  $V_i$  –  $i$ -th value of the characteristic;  $\mu_i$  – mean value of the  $i$ -th characteristic;  $N$  – size of the training sample.

In this article, data were generated for the classification of projectiles based on data from the device 1L220U: position\_x1, position\_y1, position\_h1, velocity, taget\_class, explosion\_x2, explosion\_y2, explosion\_h2, hour, minute, second, angle\_big\_tick, angle\_small\_tick, angle\_degrees, angle\_rotation\_degrees, distance\_2d, distance\_3d, flight\_time from the study [16].

Normalization (formula(6)):

$$V' = \frac{V_i - \mu_i}{\sigma_i}, \quad (6)$$

where  $V'$  – is the normalized value of the  $i$ -th characteristic;  $V_i$  – is the initial value of the  $i$ -th characteristic,  $\mu_i$  – is the mean value of the  $i$ -th characteristic,  $\sigma_i$  is the standard deviation of the  $i$ -th characteristic.

The Confusion Matrix is a tool in machine learning used to evaluate the performance of a classifier on a dataset. It shows how many elements of each class were correctly or incorrectly classified by the model.

The number of rows and columns depends on the number of labels the model is supposed to predict. In this article, the classification of 6 classes is considered, so the confusion matrix for each model will have 6 rows and 6 columns (Table 1). Each row represents instances in the actual class, and each column represents instances in the predicted class.

Table 1

The template of the confusion matrix used to construct the confusion matrix for 6 classes

Actual Class	Predicted Class	
	1 (Positive)	0 (Negative)
1 (Positive)	TP (True positive)	FN (False negative)
0 (Negative)	FP (False positive)	TN (True negative)

FN (formula (19)–(30)): the number of falsely negative classified elements for the class will be the sum of the values of the corresponding rows, except for the TP value. FP (formula (31)–(42)): the number of falsely positive classified elements for the class will be the sum of the values of the corresponding column, except for the TP value. TN (formula (43)–(48)): the number of correctly negative classified elements for the class will be the sum of all column and row values, except for the values of this class, for which we calculate the value. TP (formula (7)–(18)): the number of correctly positive classified elements, where the actual value and the predicted value match (Table 2).

Table 2

Confusion matrix for 6 classes

A	X <sub>11</sub>	X <sub>12</sub>	X <sub>13</sub>	X <sub>14</sub>	X <sub>15</sub>	X <sub>16</sub>
A/M	X <sub>21</sub>	X <sub>22</sub>	X <sub>23</sub>	X <sub>24</sub>	X <sub>25</sub>	X <sub>26</sub>
A/P	X <sub>31</sub>	X <sub>32</sub>	X <sub>33</sub>	X <sub>34</sub>	X <sub>35</sub>	X <sub>36</sub>
A/PC	X <sub>41</sub>	X <sub>42</sub>	X <sub>43</sub>	X <sub>44</sub>	X <sub>45</sub>	X <sub>46</sub>
M	X <sub>51</sub>	X <sub>52</sub>	X <sub>53</sub>	X <sub>54</sub>	X <sub>55</sub>	X <sub>56</sub>
P	X <sub>61</sub>	X <sub>62</sub>	X <sub>63</sub>	X <sub>64</sub>	X <sub>65</sub>	X <sub>66</sub>
	A	A/M	A/P	A/PC	M	P

The confusion matrix analyzes several neural network models in this work, so a detailed analysis of the confusion matrix will be conducted for the neural network with two hidden layers and the number of neurons 33 and 8 with Tanh activation functions, respectively, and an output layer with six neurons with a Softmax activation function, because this model showed the best results.

TP for class A:

$$TP_A = X_{11}, \tag{7}$$

$$TP_A = 640, \tag{8}$$

Where TP for class A/M: True Positive, meaning that the actual value and the predicted value match.

$$TP_{\frac{A}{M}} = X_{22}, \tag{9}$$

$$TP_{\frac{A}{M}} = 112, \tag{10}$$

TP for class A/P:

$$TP_{\frac{A}{P}} = X_{33}, \tag{12}$$

$$TP_{\frac{A}{P}} = 96, \tag{12a}$$

TP for class A/PC:

$$TP_{\frac{A}{PC}} = X_{44}, \tag{13}$$

$$TP_{\frac{A}{PC}} = 361, \tag{14}$$

TP for class M:

$$TP_M = X_{55}, \tag{15}$$

$$TP_M = 58, \tag{16}$$

TP for class P:

$$TP_P = X_{66}, \tag{17}$$

$$TP_P = 241, \tag{18}$$

FN for class A:

$$FN_A = X_{12} + X_{13} + X_{14} + X_{15} + X_{16}, \tag{19}$$

$$FN_A = 1 + 0 + 6 + 0 + 0 = 7, \tag{20}$$

Where FN – False Negative, meaning that the actual value is positive, but it was incorrectly predicted as negative.

FN for class A/M:

$$FN_{\frac{A}{M}} = X_{21} + X_{23} + X_{24} + X_{25} + X_{26}, \quad (21)$$

$$FN_{\frac{A}{M}} = 1 + 0 + 0 + 1 + 0 = 2, \quad (22)$$

FN for class A/P:

$$FN_{\frac{A}{P}} = X_{31} + X_{32} + X_{34} + X_{35} + X_{36}, \quad (23)$$

$$FN_{\frac{A}{P}} = 0 + 0 + 1 + 0 + 6 = 7, \quad (24)$$

FN for class A/PC:

$$FN_{\frac{A}{PC}} = X_{41} + X_{42} + X_{43} + X_{45} + X_{46}, \quad (25)$$

$$FN_{\frac{A}{PC}} = 4 + 0 + 5 + 0 + 2 = 11, \quad (26)$$

FN for class M:

$$FN_M = X_{51} + X_{52} + X_{53} + X_{54} + X_{56}, \quad (27)$$

$$FN_M = 0 + 3 + 0 + 0 + 0 = 3, \quad (28)$$

FN for class P:

$$FN_P = X_{61} + X_{62} + X_{63} + X_{64} + X_{65}, \quad (29)$$

$$FN_P = 0 + 0 + 6 + 0 + 0 = 6, \quad (30)$$

FP for class A:

$$FP_A = X_{21} + X_{31} + X_{41} + X_{51} + X_{61}, \quad (31)$$

$$FP_A = 1 + 0 + 4 + 0 + 0 = 5, \quad (32)$$

Where FP – False Positive, meaning that the actual value is negative, but it was incorrectly predicted as positive

FP for class A/M:

$$FP_{\frac{A}{M}} = X_{12} + X_{32} + X_{42} + X_{52} + X_{62}, \quad (33)$$

$$FP_{\frac{A}{M}} = 1 + 0 + 0 + 3 + 0 = 4, \quad (34)$$

FP for class A/P:

$$FP_{\frac{A}{P}} = X_{13} + X_{23} + X_{43} + X_{53} + X_{63}, \quad (35)$$

$$FP_{\frac{A}{P}} = 0 + 0 + 5 + 0 + 6 = 11, \quad (36)$$

FP for class A/PC:

$$FP_{\frac{A}{PC}} = X_{14} + X_{24} + X_{34} + X_{54} + X_{61}, \quad (37)$$

$$FP_{\frac{A}{PC}} = 6 + 0 + 1 + 0 + 0 = 7, \quad (38)$$

FP for class M:

$$FP_M = X_{15} + X_{25} + X_{35} + X_{45} + X_{65}, \quad (39)$$

$$FP_M = 0 + 1 + 0 + 0 + 0 = 1, \quad (40)$$

FP for class P:

$$FP_P = X_{16} + X_{26} + X_{36} + X_{46} + X_{56}, \quad (41)$$

$$FP_P = 0 + 0 + 6 + 2 + 0 = 8, \quad (42)$$

TN (True Negative) – the sum of values in all other rows and columns except for the class for which we are calculating the value

$$TN_A = 112 + 1 + 96 + 1 + 6 + 5 + 361 + 2 + 3 + 58 + 6 + 241 = 892, \quad (43)$$

$$TN_{\frac{A}{M}} = 640 + 6 + 1 + 4 + 5 + 361 + 2 + 58 + 6 + 241 = 1324, \quad (44)$$

$$TN_{\frac{A}{P}} = 640 + 1 + 6 + 1 + 112 + 1 + 4 + 361 + 2 + 3 + 58 + 241 = 1430, \quad (45)$$

$$TN_{\frac{A}{PC}} = 640 + 1 + 112 + 1 + 96 + 3 + 58 + 6 + 241 = 1158, \quad (46)$$



$$TN_M = 640 + 1 + 6 + 1 + 112 + 96 + 1 + 6 + 4 + 5 + 361 + 6 + 241 = 1420, \tag{47}$$

$$TN_P = 640 + 1 + 6 + 1 + 112 + 1 + 96 + 1 + 4 + 5 + 361 + 3 + 358 + 3 + 58 = 1650, \tag{48}$$

In the top left corner of the confusion matrix are the names of the actual classes. In the bottom part of the confusion matrix are the names of the predicted classes.

True	A	640	1	0	6	0	0
	AM	1	112	0	0	1	0
	AP	0	0	96	1	0	6
	A/PC	4	0	5	361	0	2
	M	0	3	0	0	58	0
	P	0	0	6	0	0	241
		A	AM	A/P	A/PC	M	P
		Predicted					

Fig. 4. Confusion matrix for MLPClassifier\_2HL\_T training dataset

After analyzing the confusion matrix, the following conclusions can be drawn for the training dataset:

1. Classification effectiveness:
  - The model showed high effectiveness in classifying certain classes, particularly “A” and “A/PC,” where the TP values are high: 640 and 361 respectively.
  - However, for some other classes, such as “A/P” and “M,” the model exhibited less satisfactory results with a noticeable number of FP and FN values.
2. Misclassification:
  - There is a certain amount of misclassified samples in all classes, indicating the model's inability to correctly identify certain subclasses.
  - The values of FP and FN for some classes indicate that the model tends to incorrectly classify some classes as others.
3. Class balance:
  - Considering the TN values, it can be understood that the model successfully identifies classes that do not belong to a specific class, except for the class for which the value is being calculated.
4. Need for further improvement:
  - Focusing on improving the classification accuracy for classes with a high number of errors (FP and FN) may enhance the overall effectiveness of the model.

Testing Set | A: 0.96 | P: 0.96 | R: 0.96 | Confusion Matrix:

True	A	152	0	0	4	0	0
	AM	0	23	0	0	1	0
	AP	0	0	23	2	0	0
	A/PC	0	0	5	83	0	0
	M	0	1	0	0	14	0
	P	0	0	2	1	0	75
		A	AM	A/P	A/PC	M	P
		Predicted					

Fig. 5. Confusion matrix for MLPClassifier\_2HL\_T test dataset



The values of accuracy: 0.96, precision: 0.96, recall: 0.96 shown in Fig. 2 above indicate that the MLPClassifier\_2HL\_T model performs with high classification effectiveness on the test dataset.

The next model to be considered is a neural network with two hidden layers and 33 and 8 neurons with Relu activation functions respectively and an output layer with six neurons with Softmax activation – MLPClassifier\_2HL\_R.

True	Predicted					
	A	A/M	A/P	A/PC	M	P
A	636	1	0	10	0	0
A/M	0	113	0	0	1	0
A/P	0	0	89	7	0	7
A/PC	5	0	4	362	0	1
M	0	2	0	0	59	0
P	0	0	11	0	0	236

Fig. 6. Confusion matrix for MLPClassifier\_2HL\_R training dataset

True	Predicted					
	A	A/M	A/P	A/PC	M	P
A	150	1	0	5	0	0
A/M	0	23	0	0	1	0
A/P	0	0	18	5	0	2
A/PC	2	0	2	84	0	0
M	0	2	0	0	13	0
P	0	0	6	1	0	71

Fig. 7. Confusion matrix for MLPClassifier\_2HL\_R test dataset

Analysis of the confusion matrix for the training and test datasets for MLPClassifier\_2HL\_R allows the following conclusions to be drawn:

1. Class “A”: MLPClassifier\_2HL\_R correctly classified 636 samples of class “A/P” in the training dataset and 150 samples in the test dataset, indicating high efficiency in classifying this class.

2. Class “A/M”: MLPClassifier\_2HL\_R also showed high efficiency in classifying samples of class “A/M” in the training dataset, correctly classifying 113 samples, but lower efficiency in the test dataset, correctly classifying only 23.

3. Class “A/P”: For the class “A/P”, MLPClassifier\_2HL\_R correctly classified 89 samples in the training dataset and 18 samples in the test dataset, indicating moderate efficiency in classifying this class.

4. Class “A/PC”: MLPClassifier\_2HL\_R correctly classified 362 samples of class “A/PC” in the training dataset and 84 samples in the test dataset, indicating average efficiency in classifying this class.

5. Class “M”: The efficiency of MLPClassifier\_2HL\_R for class “M” was lower than for other classes, correctly classifying only 59 samples in the training dataset and 13 in the test dataset.

6. Class “P”: MLPClassifier\_2HL\_R correctly classified 236 samples of class “P” in the training dataset and 71 in the test dataset, indicating high efficiency in classifying this class.

Overall, MLPClassifier\_2HL\_R has shown quite high efficiency in classifying some classes (e.g., “A” and “A/PC”), but for other classes (especially “A/P” and “M”), the results were unsatisfactory. This may require further refinement of the model to achieve better results on the test dataset.

Comparing the confusion matrix of MLPClassifier\_2HL\_R and MLPClassifier\_2HL\_T, MLPClassifier\_2HL\_R correctly classified 636 samples of class “A”, while MLPClassifier\_2HL\_T classified 640 in the training dataset; and MLPClassifier\_2HL\_R correctly classified 150 samples of class “A”, while MLPClassifier\_2HL\_T classified 152 in the test dataset, indicating high efficiency in classifying this class in both models, but MLPClassifier\_2HL\_T shows slightly better results.

Comparing the confusion matrices of the two models – MLPClassifier\_2HL\_R and MLPClassifier\_2HL\_T, we can see that both models demonstrate high efficiency in classifying dynamic objects, but MLPClassifier\_2HL\_T shows slightly better results.

The next model to be considered is a neural network with one hidden layer and 33 neurons with Relu activation function, and an output layer with six neurons with Softmax activation function – MLPClassifier\_1HL\_L.

Comparing the confusion matrix of MLPClassifier\_1HL\_L with MLPClassifier\_2HL\_T, we can see that MLPClassifier\_1HL\_L correctly classified 632 samples of class “A,” while MLPClassifier\_2HL\_T classified 640 correctly on the training dataset; and MLPClassifier\_1HL\_L correctly classified 149 samples of class “A”, while MLPClassifier\_2HL\_T classified 152 correctly on the test dataset, indicating high effectiveness in classifying this class in both models, but MLPClassifier\_2HL\_T shows slightly better results.

True	A	632	0	0	15	0	0
	A/M	0	111	0	0	3	0
	A/P	0	0	95	0	0	8
	A/PC	1	0	8	361	0	2
	M	0	1	0	0	60	0
	P	0	0	1	0	0	246
		Predicted					
		A	A/M	A/P	A/PC	M	P

Fig. 8. Confusion Matrix for MLPClassifier\_1HL\_L Training Dataset

True	A	149	0	0	7	0	0
	A/M	0	23	0	0	1	0
	A/P	0	0	21	1	0	3
	A/PC	1	0	7	80	0	0
	M	0	2	0	0	13	0
	P	0	0	0	1	0	77
		Predicted					
		A	A/M	A/P	A/PC	M	P

Fig. 9. Confusion Matrix for MLPClassifier\_1HL\_L Test Dataset

Comparing the confusion matrices of the two models – MLPClassifier\_1HL\_L and MLPClassifier\_2HL\_T, we can see that both models demonstrate high effectiveness in classifying dynamic objects, but MLPClassifier\_2HL\_T shows slightly better results.

The next model to be considered is a neural network with three hidden layers and 33 and 8 neurons with Tanh activation functions, respectively, and an output layer with six neurons with a Softmax activation function – MLPClassifier\_3HL\_T.

True	A	640	0	0	7	0	0
	A/M	0	113	0	0	1	0
	A/P	0	0	94	0	0	9
	A/PC	2	0	7	360	0	3
	M	0	1	0	0	60	0
	P	0	0	2	0	0	245
		Predicted					
		A	A/M	A/P	A/PC	M	P

Fig. 10. Confusion Matrix for MLPClassifier\_3HL\_T Training Dataset

True	A	151	0	0	5	0	0
	A/M	0	23	0	0	1	0
	A/P	0	0	24	1	0	0
	A/PC	0	0	5	83	0	0
	M	0	2	0	0	13	0
	P	0	0	1	1	0	76
		Predicted					
		A	A/M	A/P	A/PC	M	P

Fig. 11. Confusion Matrix for MLPClassifier\_3HL\_T Testing Dataset

Comparing the confusion matrix of MLPClassifier\_3HL\_T and MLPClassifier\_2HL\_T, it can be seen that MLPClassifier\_3HL\_T correctly classified 640 instances of class “A,” while MLPClassifier\_2HL\_T classified 640 correctly in the training dataset. In addition, MLPClassifier\_3HL\_T correctly classified 151 instances of class “A”, while MLPClassifier\_2HL\_T classified 152 correctly in the testing dataset, indicating high efficiency in classifying this class in both models, but MLPClassifier\_2HL\_T shows slightly better results.

Comparing the confusion matrices of the two models – MLPClassifier\_3HL\_T and MLPClassifier\_2HL\_T, both models demonstrate high efficiency in classifying dynamic objects, but MLPClassifier\_2HL\_T shows slightly better results. Additionally, MLPClassifier\_2HL\_T has two hidden

layers, while MLPClassifier\_3HL\_H has three hidden layers, so for optimizing the computational resources of the neural network, it is advisable to use a neural network with two hidden layers.

### Conclusions

Based on the analysis of the confusion matrices for the MLPClassifier models, the following detailed conclusions can be made:

1. The two-layer perceptron with Tanh activation function, MLPClassifier\_2HL\_T, shows high accuracy for classes “A” and “A/PC”, with TP values of 640 and 361 respectively.

2. The two-layer perceptron with Relu activation function, MLPClassifier\_2HL\_R, shows lower classification accuracy than the MLPClassifier\_2HL\_T model. For classes “A/P” and “M,” the results were satisfactory – 18 and 13 respectively. Compared to MLPClassifier\_2HL\_T, both models showed similar results for class “A”, but MLPClassifier\_2HL\_R showed slightly worse results.

3. The perceptron with Logistic activation function, MLPClassifier\_1HL\_L, demonstrates high classification accuracy for class “A” but less satisfactory results for some other classes. Compared to MLPClassifier\_2HL\_T, MLPClassifier\_1HL\_L shows similar effectiveness in classifying class “A,” but the results differ for other classes.

4. The three-layer perceptron with Tanh activation function, MLPClassifier\_3HL\_T, shows high classification accuracy for some classes, but the results for classes “A/P” and “M” are not satisfactory. Compared to MLPClassifier\_2HL\_T, MLPClassifier\_3HL\_T shows similar results but with greater complexity due to the third hidden layer.

Thus, the analysis based on the confusion matrix shows that the highest accuracy in classifying projectiles (A – (ammunition); A/M – (ammunition/explosive); A/P – (armor-piercing); A/PC – (armor-piercing-incendiary); M – (explosive); P – (armor-piercing ammunition)) is achieved using a neural network perceptron with the following morphology (formula (49)):

$$y_i = f_{softmax} \left( \sum_{i=1}^8 w_{li} f_{tanh} \left( \sum_{j=1}^{33} w_{ij} f_{tanh} \left( \sum_{k=1}^{18} w_{jk} x_k \right) \right) \right) \quad i \in \{1; 6\}. \quad (49)$$

So, the input sensor layer has 18 neurons because the input feature vector has 18 components; the first hidden layer has 33 neurons with Tanh activation functions; the second hidden layer has 8 neurons with Tanh activation functions; and the output layer has 6 neurons with Softmax activation functions because there are 6 objects being classified.

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## EVALUATION OF CLASSIFICATION ACCURACY USING FEEDFORWARD NEURAL NETWORK FOR DYNAMIC OBJECTS

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**Abstract.** This paper investigates the impact of the number of hidden layers, the number of neurons in these layers, and the types of activation functions on the accuracy of classifying projectiles of six types (A – (artillery); A/M – (artillery/missile); A/R – (armor-piercing); A/RC – (armor-piercing-incendiary); M – (missile); R – (armor-piercing shells)) using a multi-layer neural network, evaluated by a confusion matrix. Specifically, confusion matrices were constructed to assess the accuracy of classifying projectiles of six types (A – (artillery); A/M – (artillery/missile); A/R – (armor-piercing); A/RC – (armor-piercing-incendiary); M – (missile); R – (armor-piercing shells)) using a multi-layer perceptron with one, two, and three hidden layers and activation functions: Logistic, Tanh, Relu, Softmax, respectively. It was found that the highest accuracy in classifying projectiles is achieved using a neural network with two hidden layers, with 33 neurons in the first hidden layer with Tanh activation function and 8 neurons with Tanh activation function in the second hidden layer, and Softmax for the neurons in the output layer.

**Key words:** confusion matrix, projectile classification, neural network, computational optimization.