

Color image encryption using chaotic-based cryptosystem

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This paper presents research on a proposed project involving image encryption using a chaotic-based cryptosystem. The purpose is to create an image encryption environment with additional features derived from chaos theory. This cryptosystem applies the element of uncertainty and sensitivity to initial conditions. The encryption uses a symmetric key; generating a key is based on a chaotic map — a nonlinear mathematical function that exhibits uncertainty and randomness based on initial values. Any change in the initial conditions affects the function's outcome. Furthermore, this encryption aims to create a secure image-sharing environment over a public network, as image or text data can be intercepted or eavesdropped on by unauthorized users. A comparison based on image histogram analysis, pixel changes between the original and encrypted images, and encryption and decryption calculations were performed, demonstrating that the plain image differs from the encrypted image.

Keywords: *chaos theory; Rossler system; chaotic cryptosystem; image encryption; RGB.*

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1. Introduction

Data sharing has been the key to the success of many networked applications. In fact, the input and output data from a process need to be treated with the highest sensitivity, especially when dealing with applications involving government agencies such as military and police. The consequences of any compromise can be disastrous. This has triggered computer scientists and mathematicians to come up with the idea of masking the real message via cryptography. Cryptography is a multidisciplinary approach, formed from a combination of several academic disciplines (mathematics, computer science and electrical engineering). In order to work in this new field, the challenge is to propose a new cryptosystem that increases the security and reduces the potential for hackers to steal information [1]. Existing mathematical-based cryptosystems can be generalized into symmetric [2] and asymmetric systems [3, 4] which were founded over pure mathematics concepts. Only recently, a chaotic-based cryptosystem relying on chaotic theory was created. The chaotic system bears some properties such as sensitivity to initial conditions, topologically mixing and dense periodic orbit [5] making it a good candidate for cryptosystem [6]. A study of chaos is traced back to that of a non-linear dynamical system, which was largely applied to model real-world phenomena with the ability to predict future behavior. Many physical systems are known to be chaotic, while others were designed to be chaotic [7–16].

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Chaos was made possible for cryptography and has been greatly studied for cryptography technique [17, 18]. Some studies found that earlier cryptosystems are either inefficient in terms of performance or weak in the scale of computational complexity and security [19–21]. In order to develop a secure image encryption technique, an encryption scheme relies upon a chaotic system for key generation (for encryption), and the key is then used as a chaotic sequence for offering pixel value confusion/diffusion, and finally, an arithmetic calculation (for decryption) is required to obtain the plain image from encrypted image and key generation from the chaotic sequence.

In this work, the development of image encryption using a chaotic-based cryptosystem is demonstrated and this cryptosystem uses a three-dimensional chaotic Rossler system [22],

$$\begin{cases} \dot{x} = -y - z, \\ \dot{y} = x - ay, \\ \dot{z} = b + z(x - c). \end{cases} \quad (1)$$

The chaotic behavior of the system for parameter values $a = b = 0.2$ and $c = 5.7$ is shown in Figure 1.

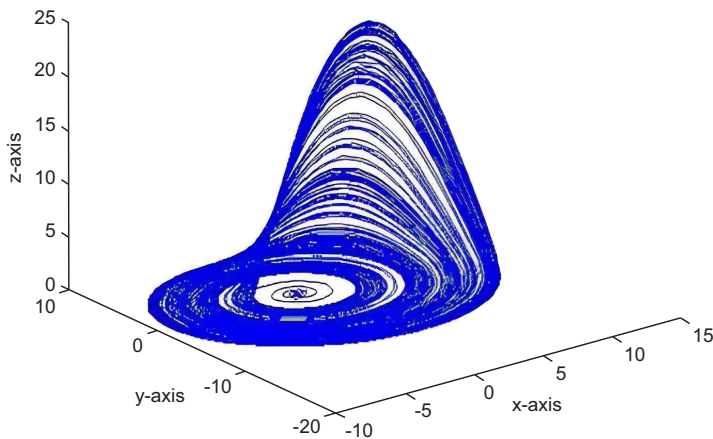


Fig. 1. Chaos attractor of the Rossler system.

This paper is structured as follows. Section 1 briefly discusses the idea of image encryption based on a chaotic cryptosystem. Section 2 reviews some related works regarding chaotic cryptography in image encryption. Section 3 exposes an idea of our proposed image encryption algorithm whereas Section 4 exposes an idea for image decryption algorithm. Finally, the summary of the research is concluded in Section 5.

2. Related works

In this section, we present some of the works related to our study. It mingles around the requirement of this new encryption technique such as image encryption, chaos theory and application of chaotic maps in cryptosystems.

The first one is a proposal for a modified version of an advanced encryption standard (AES) algorithm for image encryption. The modification focuses on the ShiftRow transformations [23]. The modified version allows cyclic left shift of ShiftRow transformation to be symmetrical and varies in numbers based on row and column. The performance analysis has been recorded from the aspects of image histogram of encrypted image, information entropy analysis and correlation coefficient of two adjacent pixels in original and encrypted image [24]. This symmetric image encryption proves that new modified version of AES exhibits a significant improvement over the original AES. The timing performance was also measured, the modified AES showed some improvements in encryption time for various image sizes (pixels) of grey-scale images.

The second technique proposed, an image encryption based on a region basis and selective part of the image [25, 26]. This technique is based on previous work that uses position permutation technique

and value transformation technique [27]. Initially, a part of an image is identified and marked for selective encryption. In this region, there occurs encryption, permutation and construction of the encryption information that will be used as a header. An implementation of chaotic key algorithm was applied for both permutation and region encryption. The timing result was recorded by varying the number of block sizes. This proposal has its advantage, once the segmentation and permutation of region are completed, the regions are independently encrypted.

A third technique uses a transformation approach where the original image is divided into a number of blocks [28]. The technique comprises two stages, dividing the image into blocks of fixed size and shuffling the blocks by applying the matrix transformation, and then applying the bit rotation algorithm. This study was extended to image encryption using pixel and position manipulation technique [29] where the pixel is shuffled by block and the row is rearranged in bit-reversed order so that the position of rows seems manipulated.

All encryption techniques we surveyed have their advantages and disadvantages [30–32]. However, in the aspect of performance, the correlation between an original image and encrypted image should be reduced and the entropy increased.

3. Proposed encryption algorithm

This proposed chaos-based image encryption algorithm scheme comprises a few steps in its execution, where the image initially goes through channel separation, where encryption takes place at an individual channel with keys generated by chaotic behavior. Each encrypted channel is finally merged before transmitting to the receiving end.

Step 1: Image Channel Separation. Plain-image goes through a channel separation process to produce a file for each individual color channel. The purpose is to segregate the pixels for Red, Green and Blue Channels. An example of channel separation is shown in Figure 2.

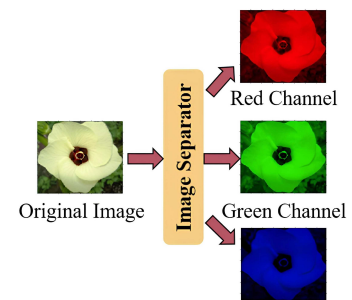


Fig. 2. Image channel separation.

Step 2: Chaos Sequence Key Generation. In this chaos sequence key generation, we used equation (1) from Rossler system. The purpose application of Rossler system in this encryption is to generate a chaos sequence to serve as encryption keys. Figure 3 shows a sequence of chaos key generation for 4 different color channels. Each column in the sequence represents Red, Green, Blue and also Alpha channels respectively.

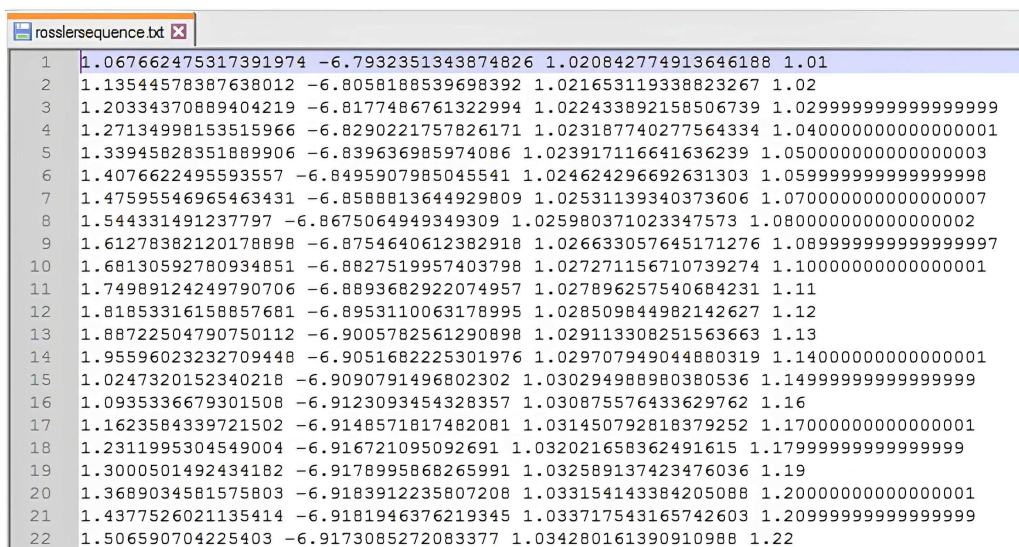


Fig. 3. Rossler's chaos sequence generation.

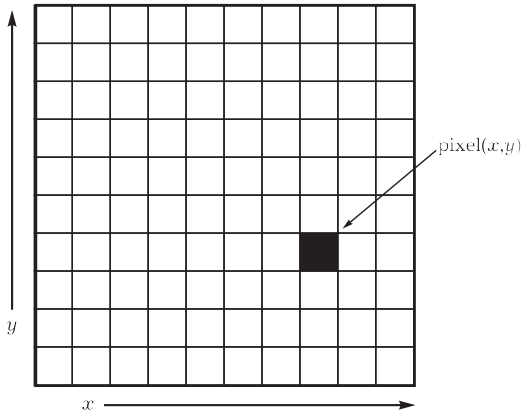


Fig. 4. Pixels illustration.

The key provided by this equation will be used throughout the processes of encryption and decryption. The encryption will take place pixel-by-pixel for each R, G, and B channels. Figure 4 shows an illustration where the encryption happened. Based on Figure 4, consider x as the row and y as the column, the encryption occurs in every image channel (x, y) where every single pixel is affected in this encryption.

Step 3: Channel Encryption. For this part, we will see how Red, Green, Blue and Alpha channels are affected by this encryption with Alpha channel taking the value of each pixel from original image. Figure 5 shows an example of encryption for the three separate channels,

$$\text{Encryption} = (\text{RosslerSequenceChannel} * 256) * (\text{NextChannel} - \text{RosslerSequenceChannel}). \quad (2)$$

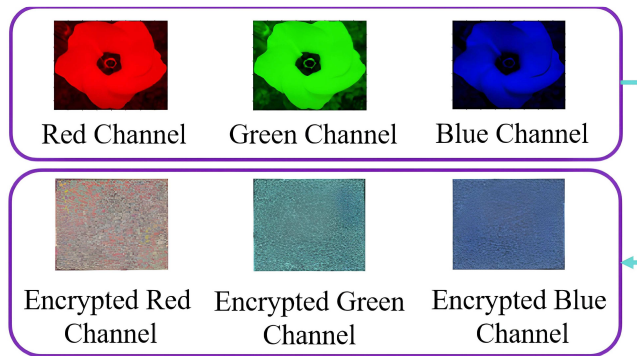


Fig. 5. Concept for encryption image channels.

The general encryption formula used is shown in equation (2). This encryption requires variables from the Rossler Sequence and pixel values from each channel. We expand the equation for each channel into the following:

$$\begin{aligned} \text{EncryptedRedChannel} &= (\text{RosslerSeqRedChannel} * 256) \\ &\quad * (\text{GreenChannel} - \text{RosslerSeqRedChannel}), \\ \text{EncryptedGreenChannel} &= (\text{RosslerSeqGreenChannel} * 256) \\ &\quad * (\text{RedChannel} - \text{RosslerSeqGreenChannel}), \\ \text{EncryptedBlueChannel} &= (\text{RosslerSeqBlueChannel} * 256) \\ &\quad * (\text{AlphaChannel} - \text{RosslerSeqBlueChannel}), \\ \text{EncryptedAlphaChannel} &= (\text{RosslerSeqAlphaChannel} * 256) \\ &\quad * (\text{BlueChannel} - \text{RosslerSeqAlphaChannel}). \end{aligned} \quad (3)$$

Let us use the pixel value at (1, 1) from Figure 6 and apply in detailed formula presented in equation (3).

By using the data from the first line of Rossler's Chaos Sequence Generation shown in Figure 3 and the channel values taken from Figure 6, we come to the following values,

$$\begin{aligned} \text{EncryptedRedChannel} &: (1.0676625 * 256) * (137 - 1.0676625) = 36855, \\ \text{EncryptedGreenChannel} &: (-6.7932353 * 256) * (226 - (-6.7932353)) = -403448, \\ \text{EncryptedBlueChannel} &: (1.0208428 * 256) * (125 - 1.0208428) = 66033, \\ \text{EncryptedAlphaChannel} &: (1.01 * 256) * (255 - 1.01) = 31734. \end{aligned} \quad (4)$$

This process takes place for every single pixel for each channel in the image, where the performance of encryption depends on how much pixel is being processed in order to encrypt the image.



Fig. 6. Pixel (1, 1) representation for Lena .png.

Step 4: Image Channel Merger. After each pixel has been encrypted, the encrypted image for each channel will look like Figure 7. Then all three image channels will be merged together to create an encrypted image in a complete RGB Channels as shown in Figure 7.

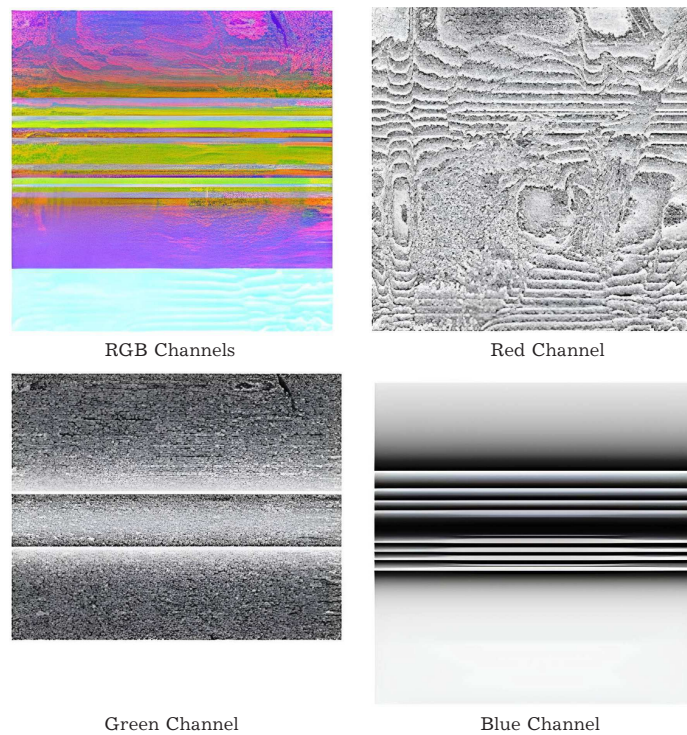


Fig. 7. Lena .png after encryption in 3 different channels.

Step 5: Cipher-Image and Key Distribution. As the process for Image Channels Merger is completed, the user will obtain two files, the encrypted images and the key. These two are compulsory in order to decrypt the encrypted image by the receiver. Figure 8 illustrated a general understanding of the encryption process.



Fig. 8. Overview for cipher-image and key distribution.

4. Proposed decryption algorithm

Decryption is a reverse process in order to acquire the original image from an encrypted image using the key that has been distributed. Since this cryptosystem is based on symmetric key encryption, the encrypted image can only be decrypted using the key as used for encryption. The steps required in the decryption process are, acquiring the encrypted image accompanied with the key that has been distributed, image channel separation, reverse channel encryption, and image channel merging to recover the original image.

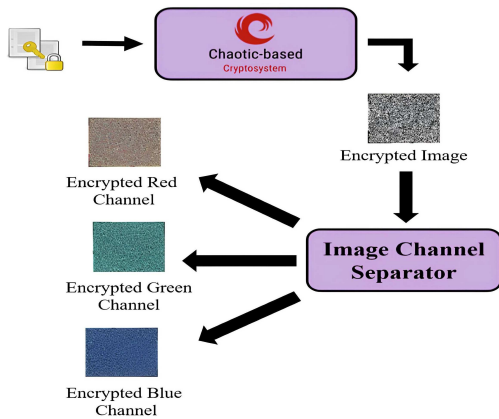


Fig. 9. Operation for input cipher-image, key and image channel separation.

Step 1: Input Cipher-image, Key and Image Channel Separation. The first step shown in Figure 9 is about collecting encrypted images, and a symmetric key accompanied with. The validation process takes a turn where a header from the key will recognize their encrypted image. After that, the image channel separation process will be executed before the decryption algorithm is executed.

Step 2: Reverse Channel Encryption. Equation (5) shows the reverse encryption (decryption) calculation where the calculation can retrieve the original pixel that has been encrypted using equation (2),

$$\text{Decryption} = \text{EncryptedNextChannel} / (\text{RosslerSequenceNextChannel} * 256) + \text{RosslerSequenceNextChannel} \tag{5}$$

This decryption requires variables from the Rossler Sequence and encrypted pixel values from each channel. We expand the equation for each channel into the following:

$$\begin{aligned} \text{DecryptedRed} &= \text{EncryptedGreen} / (\text{RosslerSeqGreen} * 256) + \text{RosslerSeqGreen}, \\ \text{DecryptedGreen} &= \text{EncryptedRed} / (\text{RosslerSeqRed} * 256) + \text{RosslerSeqRed}, \\ \text{DecryptedBlue} &= \text{EncryptedAlpha} / (\text{RosslerSeqAlpha} * 256) + \text{RosslerSeqAlpha}, \\ \text{DecryptedAlpha} &= \text{EncryptedBlue} / (\text{RosslerSeqBlue} * 256) + \text{RosslerSeqBlue}. \end{aligned} \tag{6}$$

A further calculation that uses variables from encrypted channel values produces the following,

$$\begin{aligned} \text{DecryptedRedChannel} &: -403448 / (-6.7932353 * 256) + (-6.7932353), \\ \text{DecryptedGreenChannel} &: 36855 / (1.0676625 * 256) + (1.0676625), \\ \text{DecryptedBlueChannel} &: 31734 / (1.01 * 256) + (1.01), \\ \text{DecryptedAlphaChannel} &: 66033 / (1.0208428 * 256) + (1.0208428). \end{aligned} \tag{7}$$

When the decryption process is done for all channels, it produces 3 images in 3 different channels.

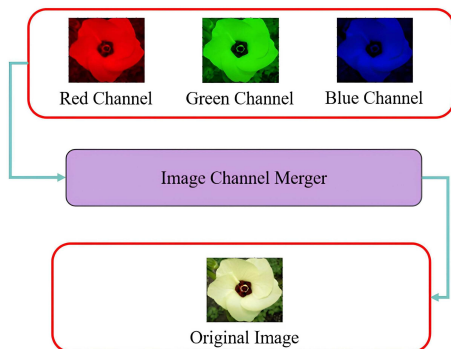


Fig. 10. Operation for Image Channel Merger.



Fig. 11. Lena.png after Decryption in 3 Different Channels.

Step 3: Image Channel Merger and Plain-image. From the decryption process, the 3 channels are merged to create a single plain image which must be identical to the original image. The idea is to produce a plain image with RGB channels merged as shown in Figure 10.

Back to the decryption performed on `Lena.png`, Figure 11 shows the outcome of the decryption process. After individual channels have been merged, it produces the `Lena.png` in RGB channels intact together as a plain image.

5. Image analysis for encrypted image

This section discusses the two types of image analysis, image channel analysis and image histogram analysis.

5.1. Image channel analysis

In this analysis, the purpose is to observe how much the encryption process affects the pixel formation for each channel. The image to be analyzed is the encrypted image shown in Figure 12. The image channel analysis is performed in the ImageJ application. The result of the image analysis is shown in Figure 13. This analysis proved that every single encryption that occurred in the channels does not have any correlation between each pixel in different channels.



Fig. 12. Encrypted Image of *Lena.png*.

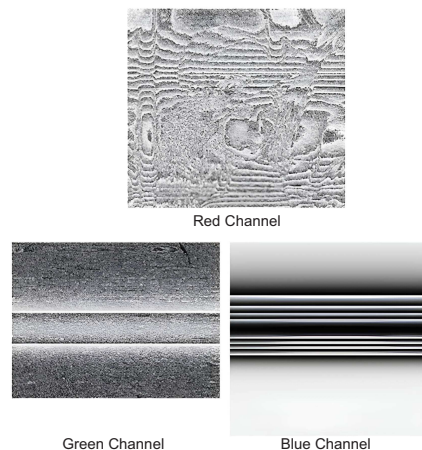


Fig. 13. Encrypted Channels of *Lena.png*.

5.2. Image histogram analysis

Image histogram analysis is the practice of studying and analyzing the context of the image via pixel density value. The pixel density is measured by the tonal value from 0 to 255 and how frequently does it occur in the image. The purpose is to show that the Histogram for the original image and the encrypted image do not match in terms of pixel density and tonal value frequency. Figures 14 and 15 show the histogram analysis of the grayscale version of *Lena.png* for the original image and encrypted image respectively.

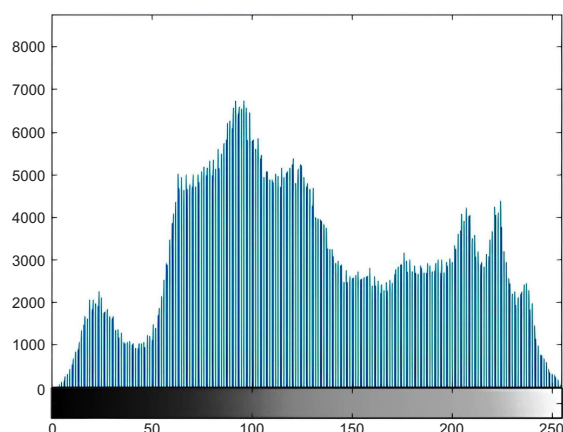


Fig. 14. Original Image — Grayscale Histogram Analysis.

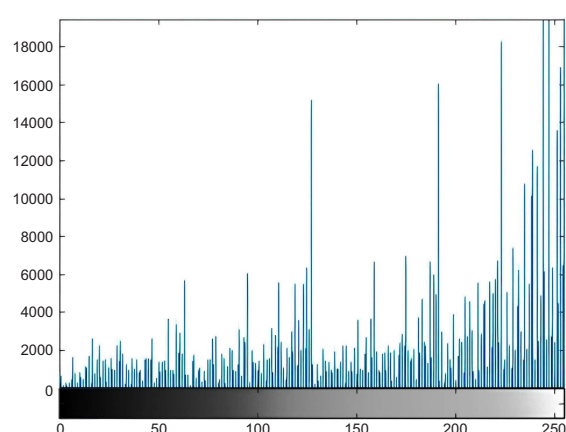


Fig. 15. Encrypted Image — Grayscale Histogram Analysis.

It is observable that there are no major similarities found in both histograms. Moreover, image histogram analysis for RGB channels is also performed. Figures 16 and 17 show the histogram for RGB channels for the original image and the encrypted image, respectively.

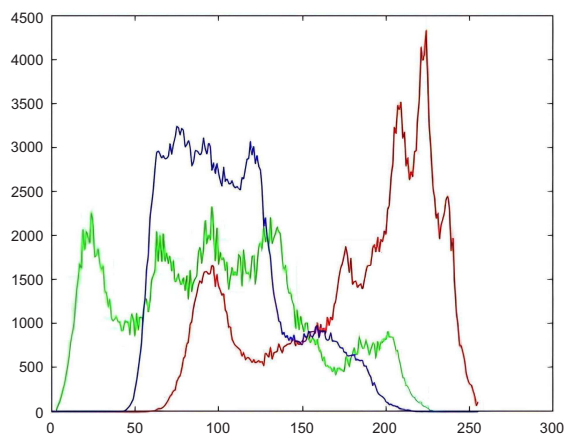


Fig. 16. Original Image — RGB Channels Histogram Analysis.

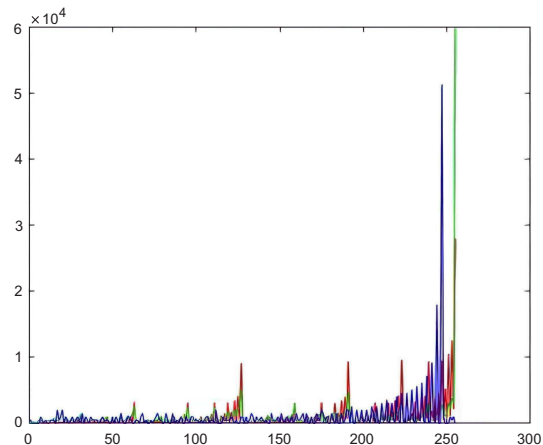


Fig. 17. Encrypted Image — RGB Channels Histogram Analysis.

6. Conclusion

This research focuses on the study of image encryption using a chaotic-based cryptosystem to ensure the confidentiality of the image is retained. We implemented the Rossler Equation where we use the Rossler Sequence to generate numbers to be used as variables to encrypt each color channel of an image. The result reveals the contribution of this paper.

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Шифрування кольорового зображення за допомогою хаотичної криптосистеми

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У цій роботі представлено дослідження запропонованого проекту, що передбачає шифрування зображень за допомогою хаотичної криптосистеми. Мета полягає в тому, щоб створити середовище шифрування зображень з додатковими функціями, отриманими з теорії хаосу. Ця криптосистема застосовує елемент невизначеності та чутливості до початкових умов. Шифрування використовує симетричний ключ; генерування ключа базується на хаотичній карті — нелінійній математичній функції, яка виявляє невизначеність і випадковість на основі початкових значень. Будь-яка зміна початкових умов впливає на результат функції. Крім того, це шифрування спрямоване на створення безпечного середовища для обміну зображеннями через загальнодоступну мережу, оскільки зображення або текстові дані можуть бути перехоплені або підслухані неавторизованими користувачами. Порівняння на основі аналізу гістограми зображення, зміни пікселів між вихідним і зашифрованим зображеннями, а також розрахунків шифрування та дешифрування було виконано, демонструючи, що звичайне зображення відрізняється від зашифрованого зображення.

Ключові слова: теорія хаосу; система Росслера; хаотична криптосистема; шифрування зображень; RGB.